

# Moon formation of rocky/icy planets by a giant impact

**Shigeru Ida**  
(ELSI, Tokyo Tech)

Ida, Ueta, Sasaki, Ishizawa (2020, Nature Astron.)

Nakajima, Genda, Asphaug, Ida (2022, Nature Comm.)

# Back-ground: How common are large moons around rocky or icy exoplanets?

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- Earth's Moon → control Earth's climate → **one possible factor of habitability?**
    - control Earth's obliquity and spin period evolution; mix deep ocean water
  - Standard Moon formation model: **giant impact model**
    - Final phase of rocky planet accretion is "giant impacts" : energetic collisions between protoplanets formed by "oligarchic growth" (Kokubo & Ida 1998)
    - In many cases, a "large" moon is formed as a by-product such as Earth's Moon?  
 $M_{\text{Moon}} \sim 0.01 M_{\text{Earth}}$
  - Other planets in Solar system?
    - **Venus**: retrograde impact → planet spin & moon: retrograde  
→ the moon falls onto the planet by tidal orbital evolution (Atobe & Ida 1997)
    - **Mercury & Mars**: left-over protoplanets that avoided giant impacts? (Hansen 2009)
    - **Uranus**: tilted by 98 degree ← giant impact
- **Large exo-moons: common around exoplanets?**  
**But, transit timing/duration variation observation (e.g., HEK): no detection**

# Back-ground: Mysteries of Uranian moon system

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## ■ Earth:

- impact by protoplanet with  $\sim 0.1 M_{\text{planet}}$  (consistent with oligarchic growth model)
  - $\sim 0.02 M_{\text{planet}}$  debris disk (e.g., Canup & Asphaug 2001, Nature)
  - $\sim 0.01 M_{\text{planet}}$  single moon (Ida, Canup & Stewart 1997, Nature)

**succeeded to reproduce Earth's Moon**

(except the identical isotope ratios)

## ■ Uranus:

- spin axis is tilted by 98 degrees ← giant impact: likely
- 17 hour spin period →  $\sim 0.1 M_{\text{planet}}$  impact
  - $\sim O(0.01) M_{\text{planet}}$  debris disk →  $\sim 0.01 M_{\text{planet}}$  **single moon?**

**NO: four small major moons  $\sim 10^{-4} - 10^{-5} M_{\text{planet}}$**

→ moons were formed in a different way?

# Back-ground: Mysteries of Uranian moon system



## ■ Uranus

➤ **both spin axis & moons' orbits: tilted by 98 degrees**

## ■ moon accretion in CircumPlanetary gas Disk? (Szulágyi et al. 2018)

➤ ~10 wt.% gas envelope → moons: accreted in the CPD?  
→ moons' orbital plane ~ planetary orbital plane

➤ How to tilt the spin axis and moons' orbits?

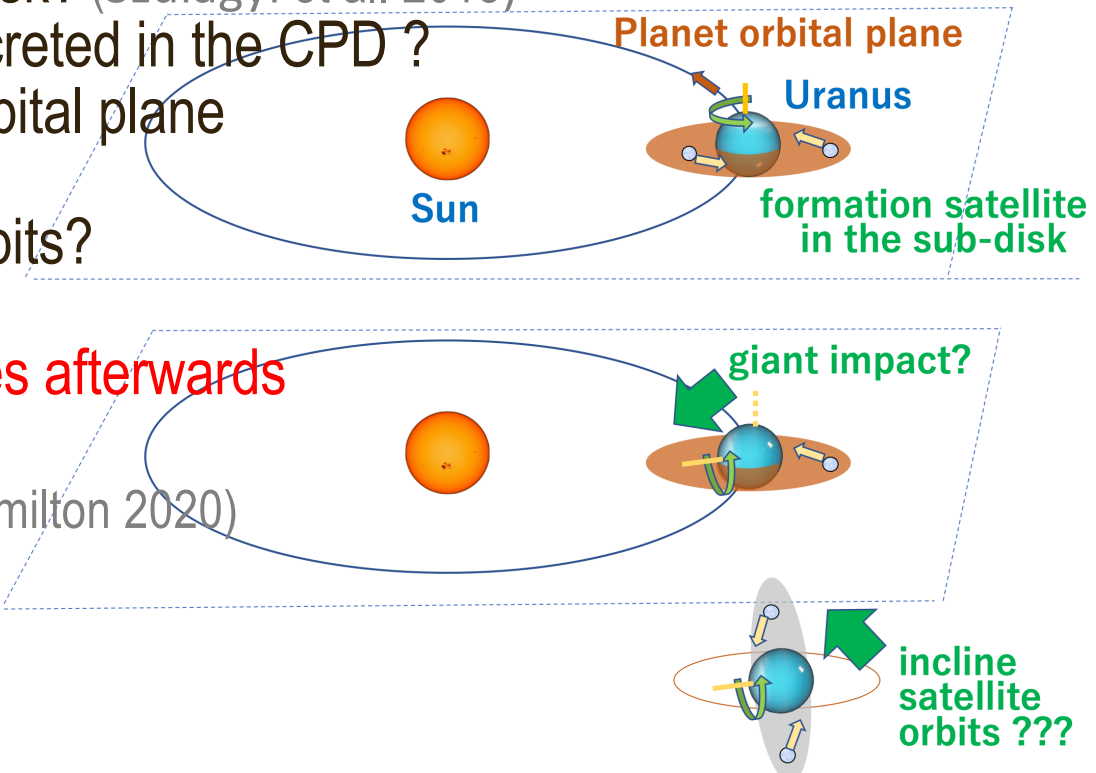
✓ A giant impact (instantaneously)

**hard to incline the moon orbital planes afterwards**

✓ Spin-orbit resonance (secular)

(Boue & Laskar 2010, Rogoszinski & Hamilton 2020)

**hard to incline by > 90 degrees**

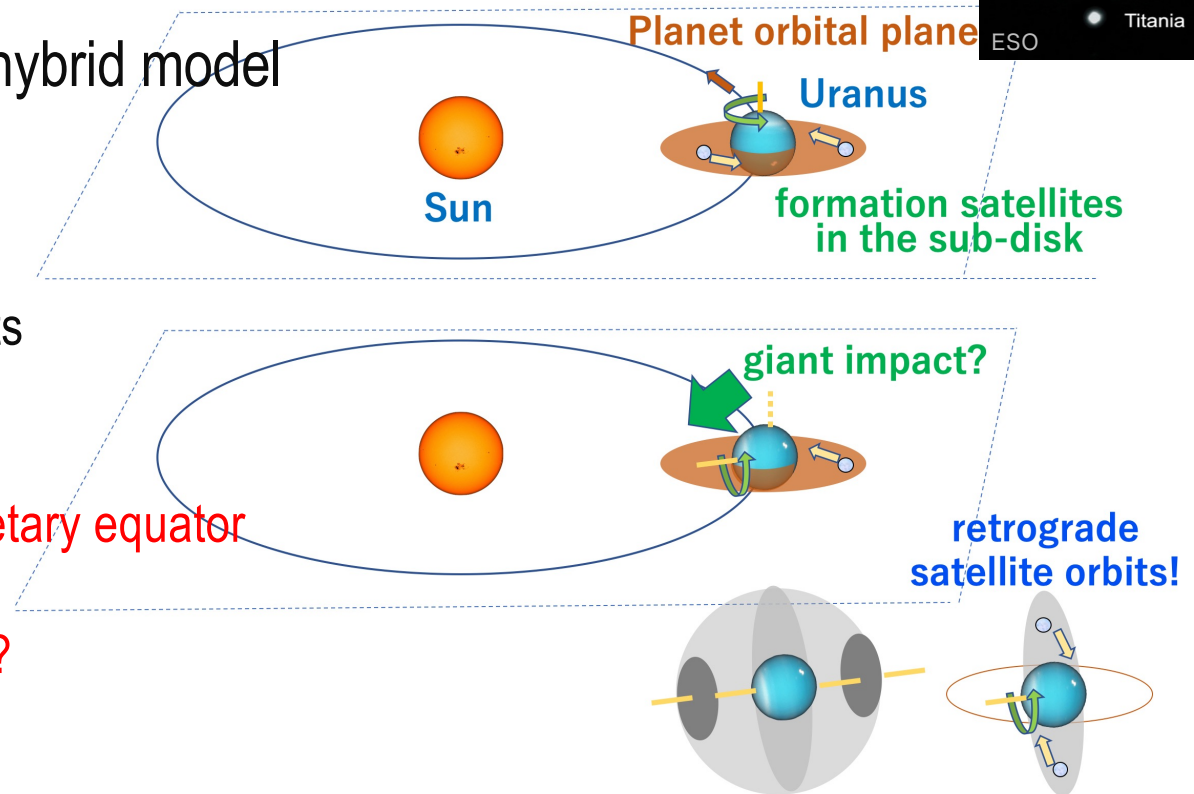


# Back-ground: Mysteries of Uranian moon system



➤ Morbidelli et al. (2012)  
-- clever, complicated, multi-step hybrid model

1. Protomoons form in a CPD
2. Giant impact tilts the spin
  - Protomoon orbits are not inclined
3. Nodal precession of protomoon orbits along tilted spin axis → thick torus
4. Collisional damping
  - Debris orbits: align the tilted planetary equator
5. Re-accreted moons – Retrograde!
  - Multiple giant impacts??

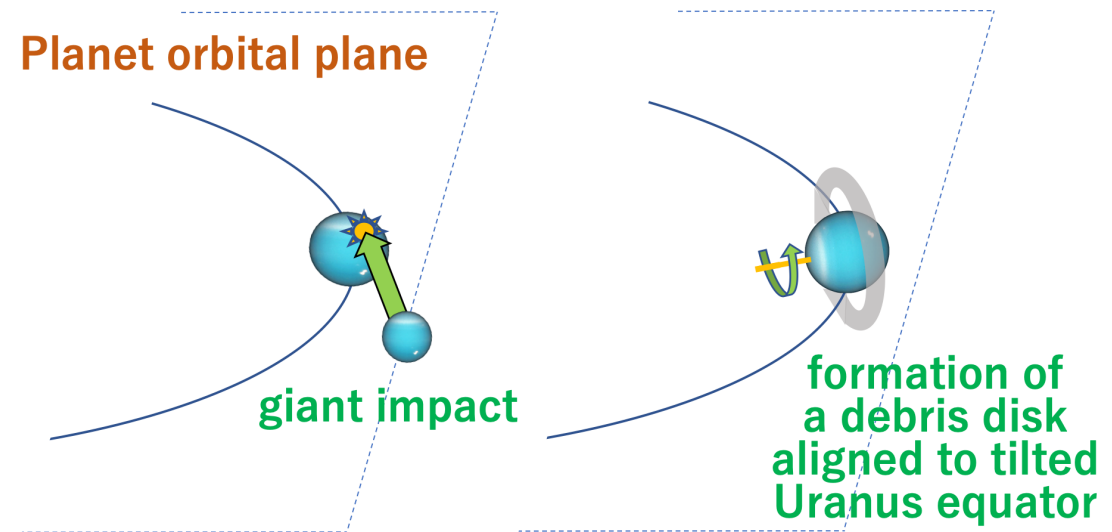


# Back-ground: Mysteries of Uranian moon system



- A single-impact model: accretion of moons from **an impact debris disk?**
  - The giant impact onto slowly spinning Uranus: naturally forms the tilted spin and **a similarly inclined prograde satellite system.**

Much more simple



# Problems in the single impact model

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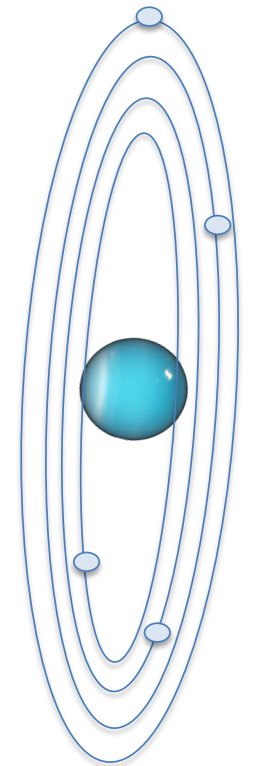
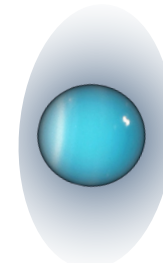
- impact: constrained by the current spin period
  - oblique,  $M \sim 0.1 M_{\text{J}}$  (consistent with oligarchic growth model)

- **Disks predicted by giant impact simulated by SPH**

Slattery et al. (1992), Kegerreis et al. (2018),

Kurosaki et al. (2019), Reinhardt et al. (2020)

- 10 x more compact ( $\sim 2r_{\text{J}}$ ), 100 x heavier disk ( $\sim 10^{-2}M_{\text{J}}$ ) than the current moon systems
  - ✓ Tidal orbital expansion afterward: not effective Dermott et al. (1988)
- almost no rock component:
  - ✓ rocks : central part as a core ← oblique impact
  - ➔ inconsistent with current moons (half rock + half ice) !



**The single impact model: inconsistent?**

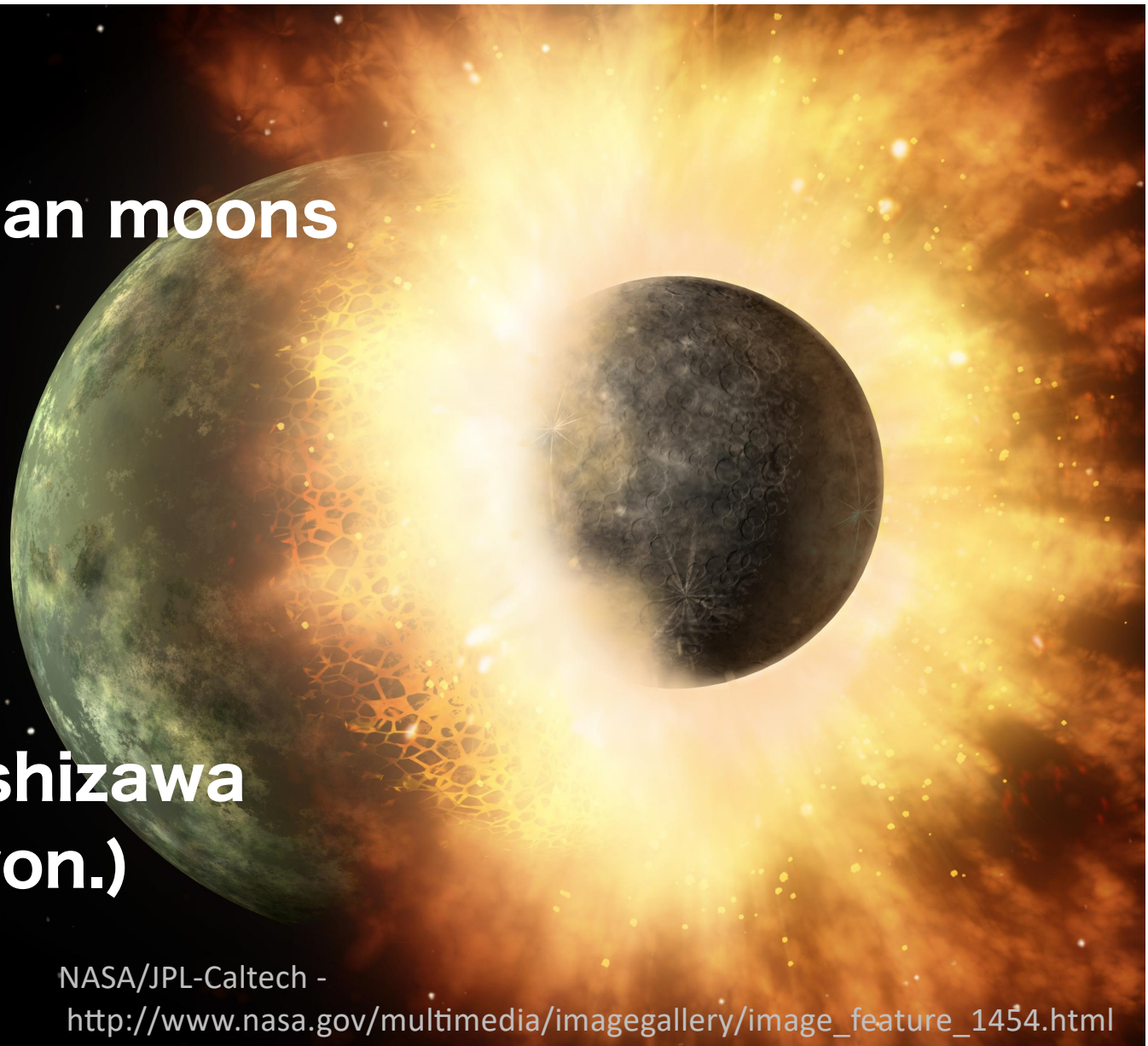


# Formation of Uranian moons by a giant impact

Ida, Ueta, Sasaki, Ishizawa  
(2020, Nature Astron.)

NASA/JPL-Caltech -

[http://www.nasa.gov/multimedia/imagegallery/image\\_feature\\_1454.html](http://www.nasa.gov/multimedia/imagegallery/image_feature_1454.html)





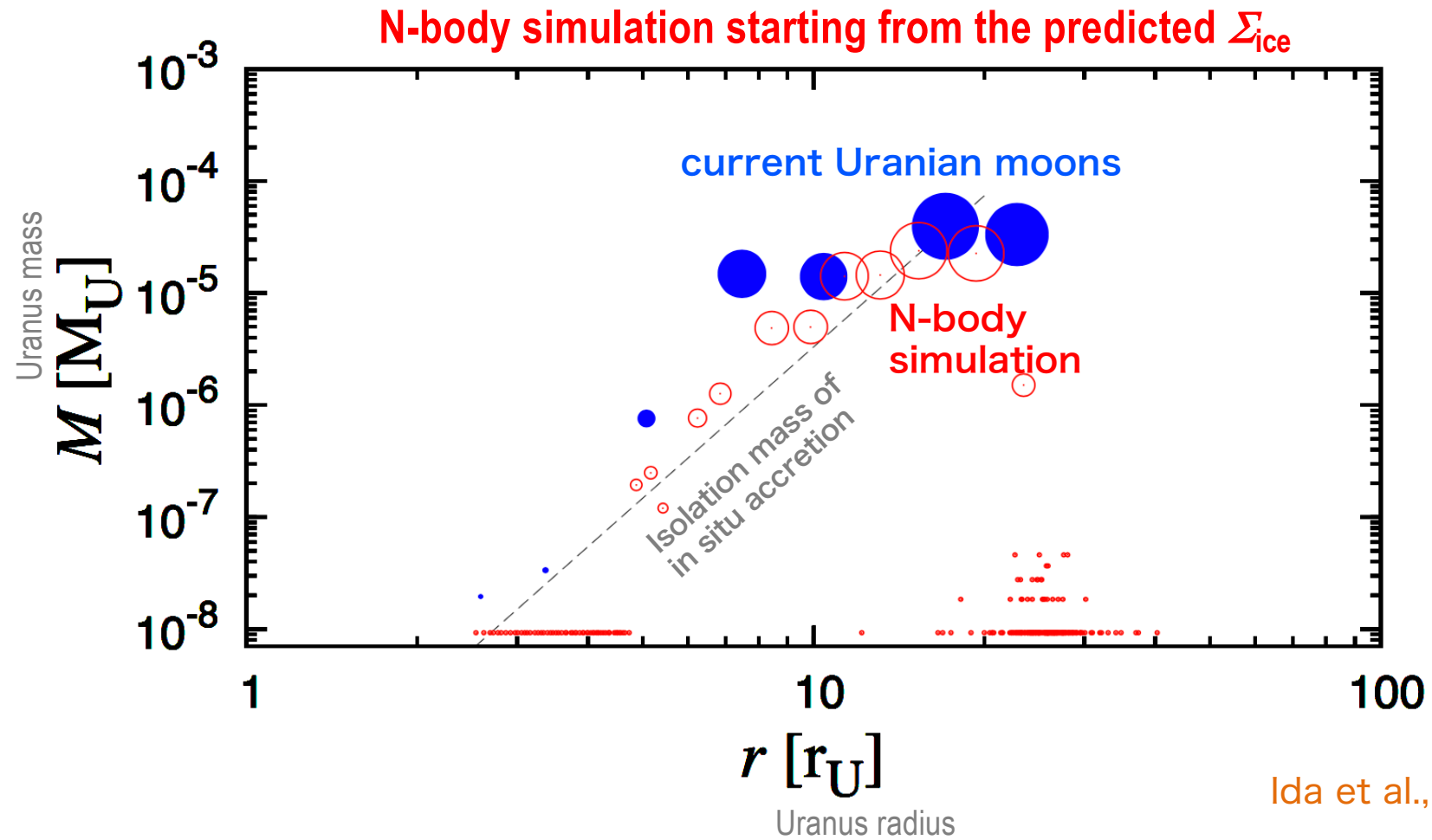
# Conclusion in advance

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Giant impact -- debris disk: too massive (x100), too compact (x10), too low rock/ice

- Debris disk: **water vapor** + H/He gas
  - **vaporized**: low vaporization temperature of H<sub>2</sub>O, high impact velocity to Uranus
  - **substantial viscous disk evolution until re-condensation of H<sub>2</sub>O**
    - **only 1% of initial  $M_{\text{disk,vapor}}$  remains**
    - **size spreading by x10** ~ **the current satellites**
- $\Sigma_{\text{ice}} \propto r^{3/2} \leftarrow$  viscous heating: inefficient in outer region
  - In situ moon accretion  $\leftarrow$  low density of H/He gas
    - **larger moons in outer region** ~ **the current satellites**
- **rock/ice ratio: enhanced** ( $\leftarrow$  high condensation temperature of silicates)

# Reproduction of the current satellites



# Disk evolution

We performed 1D diffusion calc.  
with constant  $\alpha$  & viscous heating

$$(T \propto \Sigma_{\text{disk}}^{1/3} r^{-1/2})$$

➤ ice condensation:

✓  $T \sim 240\text{K}$

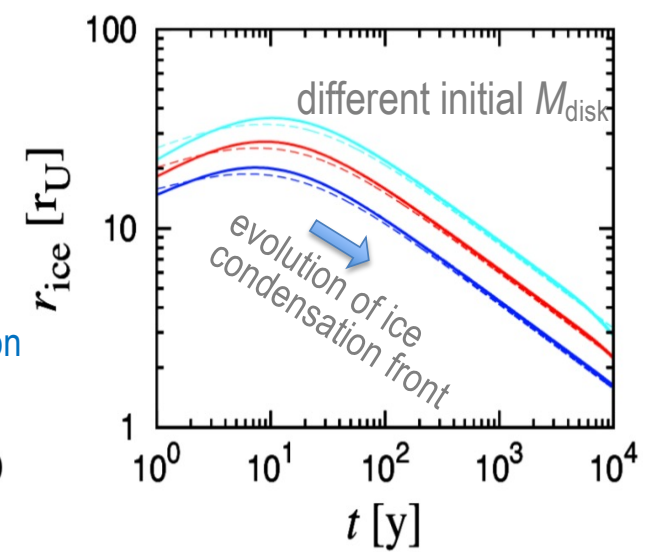
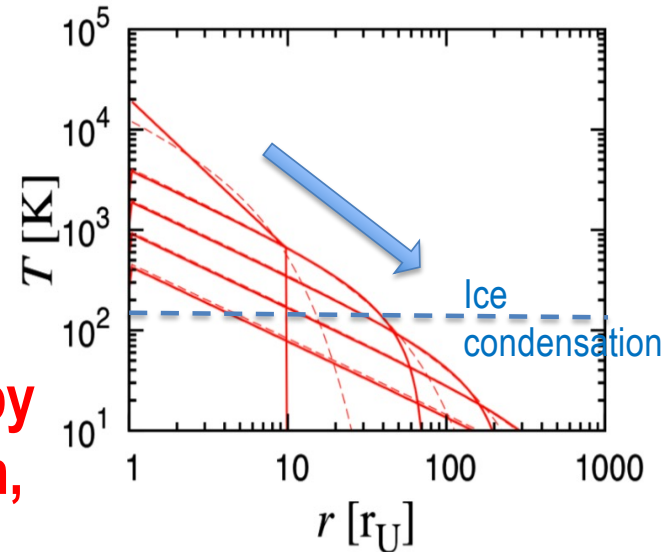
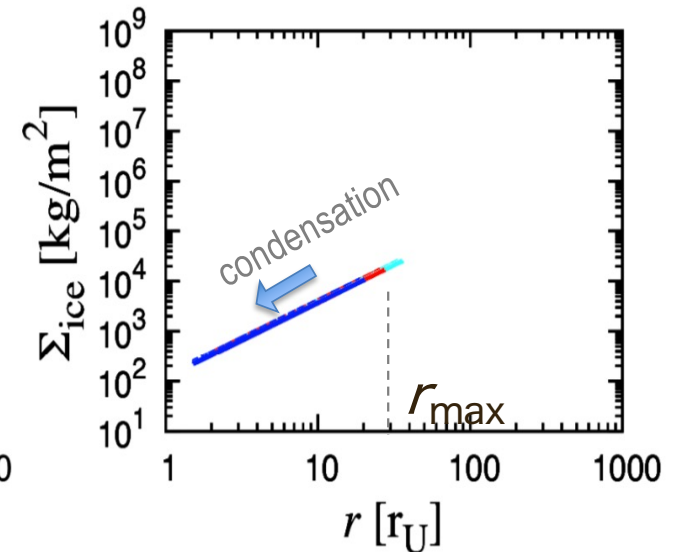
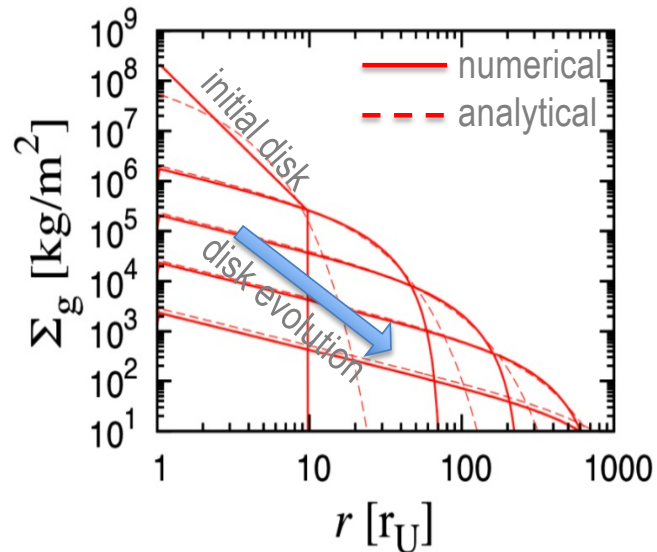
→ threshold  $\Sigma_{\text{disk}} \propto r^{3/2}$

→  $\Sigma_{\text{ice}} \propto r^{3/2}$

**indep. of the initial disk**

✓ outside-in manner

**Final moon mass is determined by  
disk evolution until condensation,  
not by initial disk mass.**



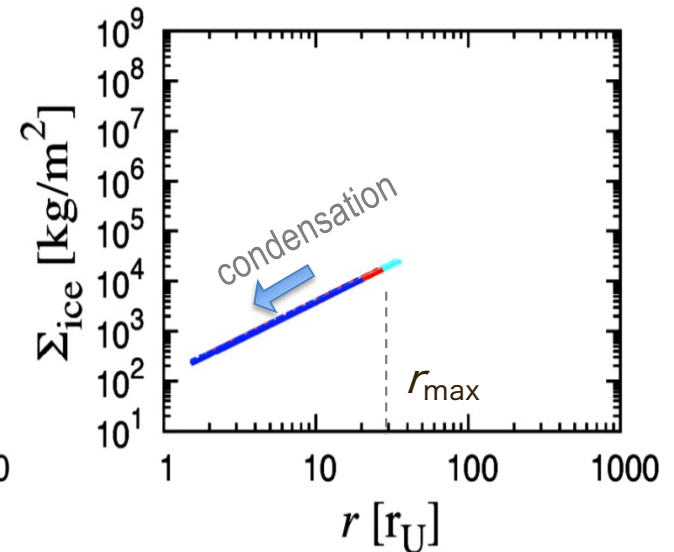
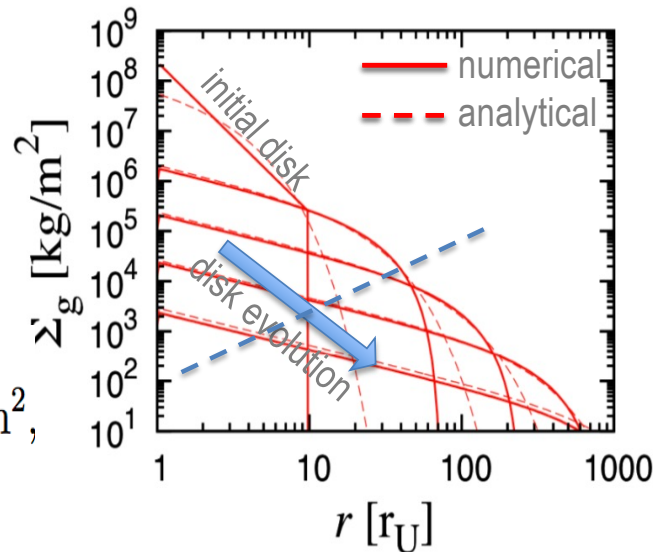
# Ice condensation

-- condensed ice surface density

$$\Sigma_{\text{ice}} \simeq \gamma \Sigma_{\text{g}} \simeq 1.2 \times 10^2 \beta^{-1} \gamma_{03} \left( \frac{r}{r_{\text{U}}} \right)^{3/2} \text{ kg/m}^2,$$

$$\beta = (\alpha/10^{-3})$$

$$\gamma_{03} = (\text{water vapor fraction})/0.3$$



-- ice distribution extent ← initial  $M, L$  of the impact-generated disk

$$r_{\text{max}} \simeq 20 \left[ \beta \left( \frac{\langle r_{\text{d,imp}} \rangle}{2 r_{\text{U}}} \right)^{-5/4} \left( \frac{M_{\text{d,imp}}}{10^{-2} M_{\text{U}}} \right) \right]^{1/4} r_{\text{U}}$$

$M_{\text{d,imp}}$ : initial debris disk mass

$\langle r_{\text{d,imp}} \rangle = ((J_{\text{d,imp}}/M_{\text{d,imp}})/r_{\text{U}}^2 \Omega_{\text{U}})^2 r_{\text{U}}$ : initial disk radius

← intersection of envelope of  $\Sigma_{\text{disk}}$  and ice condensation  $\Sigma_{\text{ice}}$

$2 r_{\text{U}}$  – viscous spreading →  $20 r_{\text{U}}$

↔ current satellites  $a < 22.8 r_{\text{U}}$

**x 10 expansion** weak dependence on initial disk

# Ice condensation

-- total mass of condensed ice

$$M_{\text{ice}} \simeq \int_{r_U}^{r_{\text{max}}} 2\pi r \Sigma_{\text{ice}} dr \simeq 0.58 \times 10^{-4} \beta^{1/8} \gamma_{03} \left( \frac{\langle r_{\text{d,imp}} \rangle}{2 r_U} \right)^{-5/4} \left( \frac{M_{\text{d,imp}}}{10^{-2} M_U} \right)^{7/8} M_U$$

$$\beta = (\alpha/10^{-3})$$

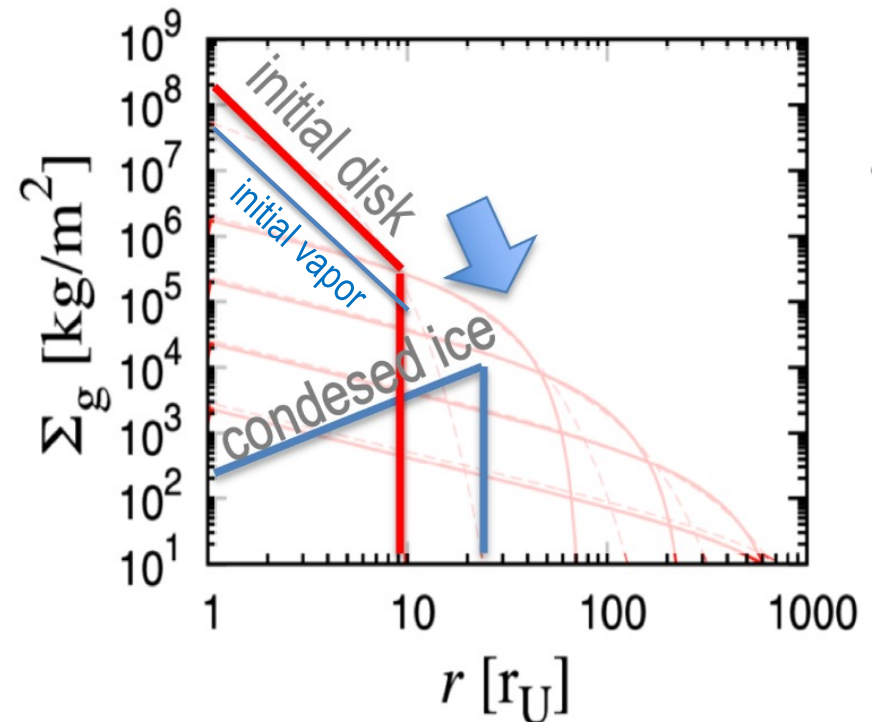
$M_{\text{d,imp}}$ : initial debris disk mass,

$r_{\text{d,imp}}$ : initial debris disk radius

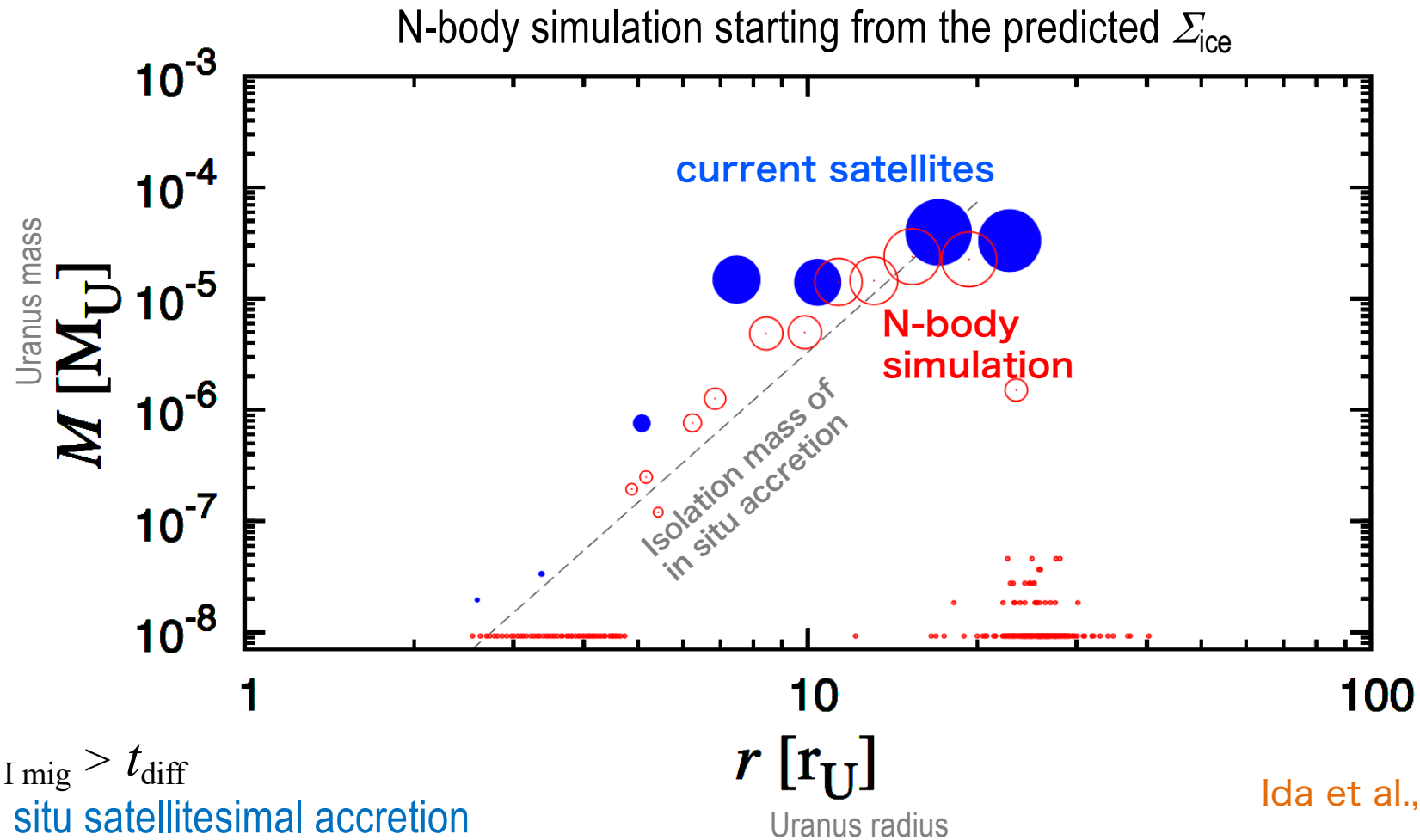
$10^{-2} M_U$  – viscous diffusion  $\rightarrow 10^{-4} M_U$  **x 1/100**  
 $\leftrightarrow$  current moons  $M_{\text{tot}} \sim 10^{-4} M_U$

-- in situ moon accretion

$$t_{\text{grow}} \ll t_{\text{drift}} \ll t_{\text{diff}}$$



# Reproduction of the current satellites



$t_{\text{type I mig}} > t_{\text{diff}}$   
→ in situ satellitesimal accretion

Ida et al., 2020

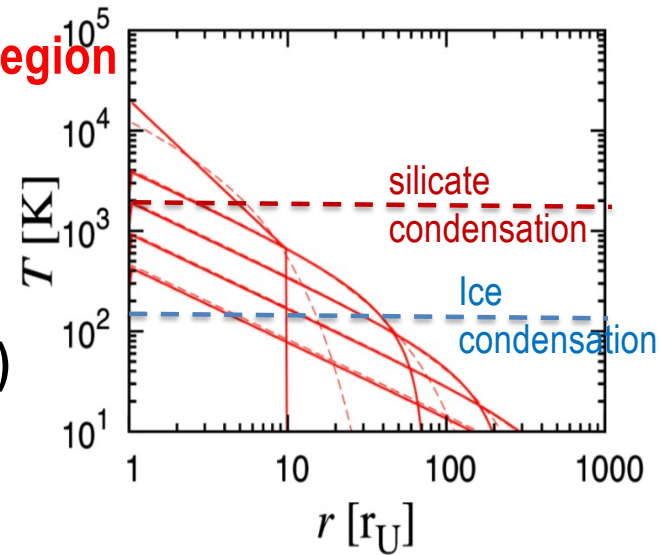
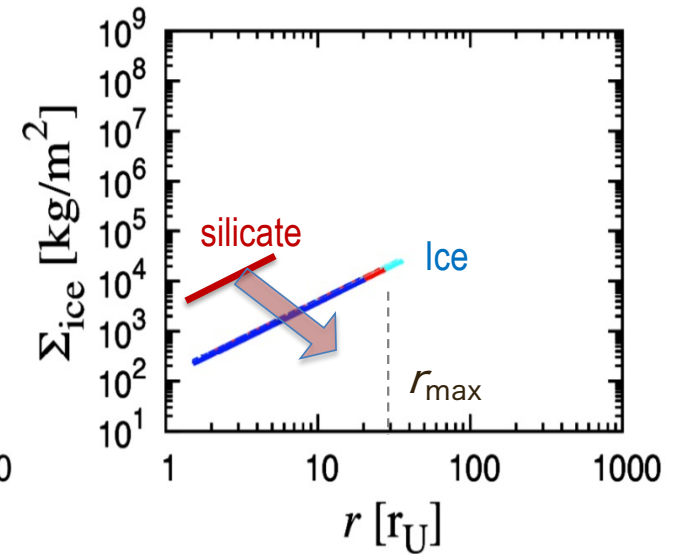
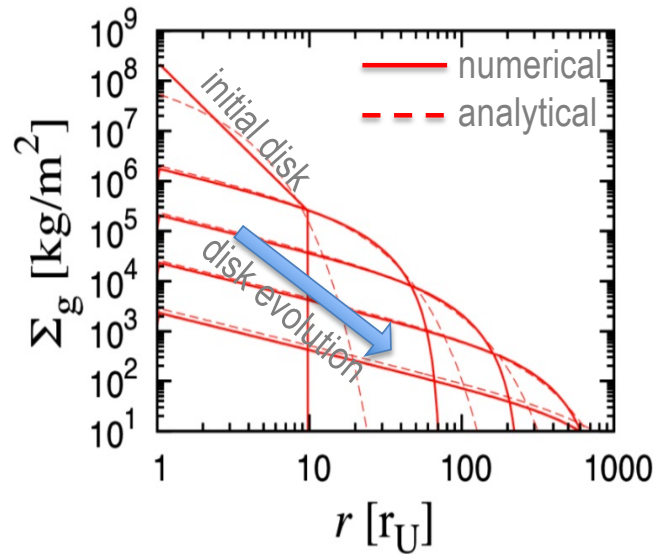
# Enhancement of rock/ice ratio

## ■ silicates

- higher condensation  $T$ 
  - **earlier condensation than ice**
- do not grow (less sticky)
  - viscous spreading with gas
- **after ice condensation,**  
**stick to the icy particles in outer region**

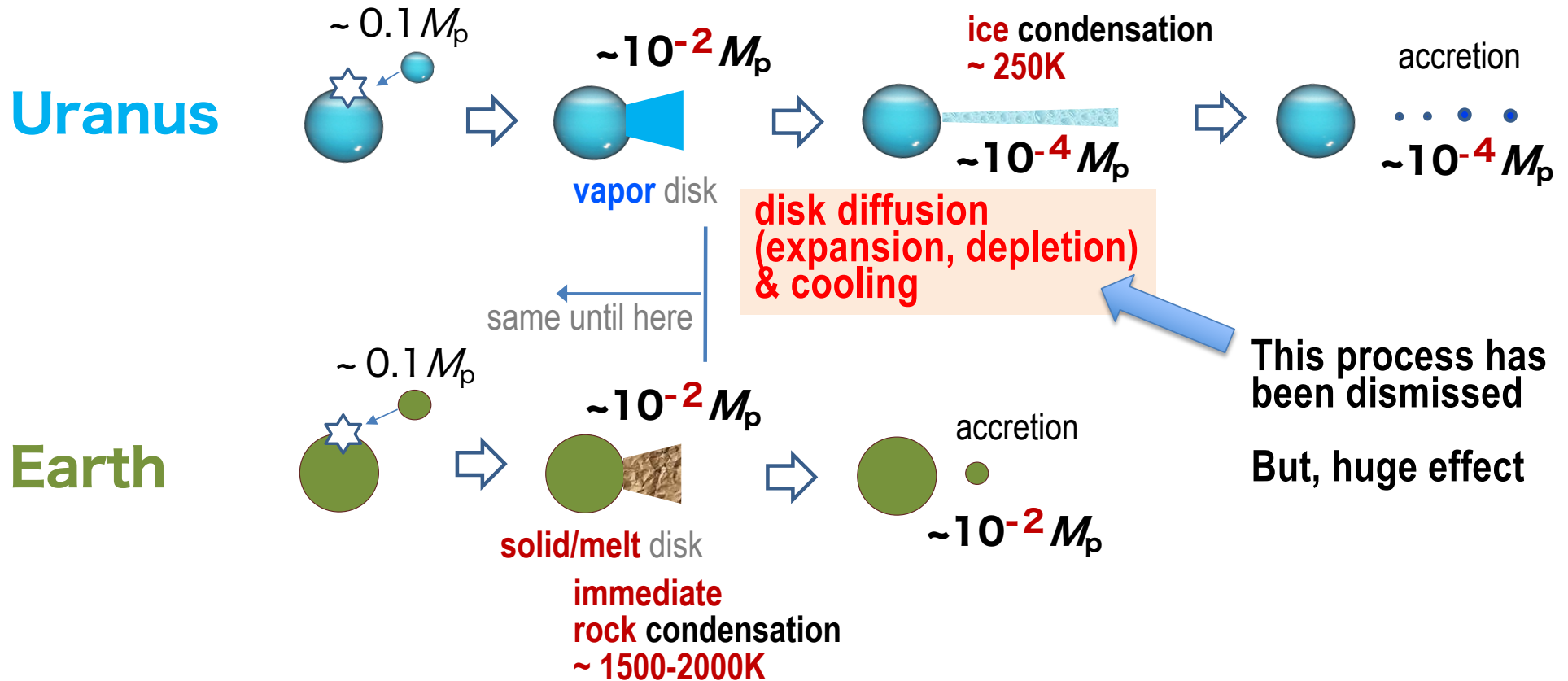
→  $\Sigma_{\text{silicate}} / \Sigma_{\text{ice}}$  [condense]  
 >>  $\Sigma_{\text{silicate}} / \Sigma_{\text{ice}}$  [initial]

potentially explains  $\Sigma_{\text{silicate}} / \Sigma_{\text{ice}} \sim \mathcal{O}(1)$   
 of the current moons, produced from  
 ice-rich body impact





# Summary of Ida et al.(2020)



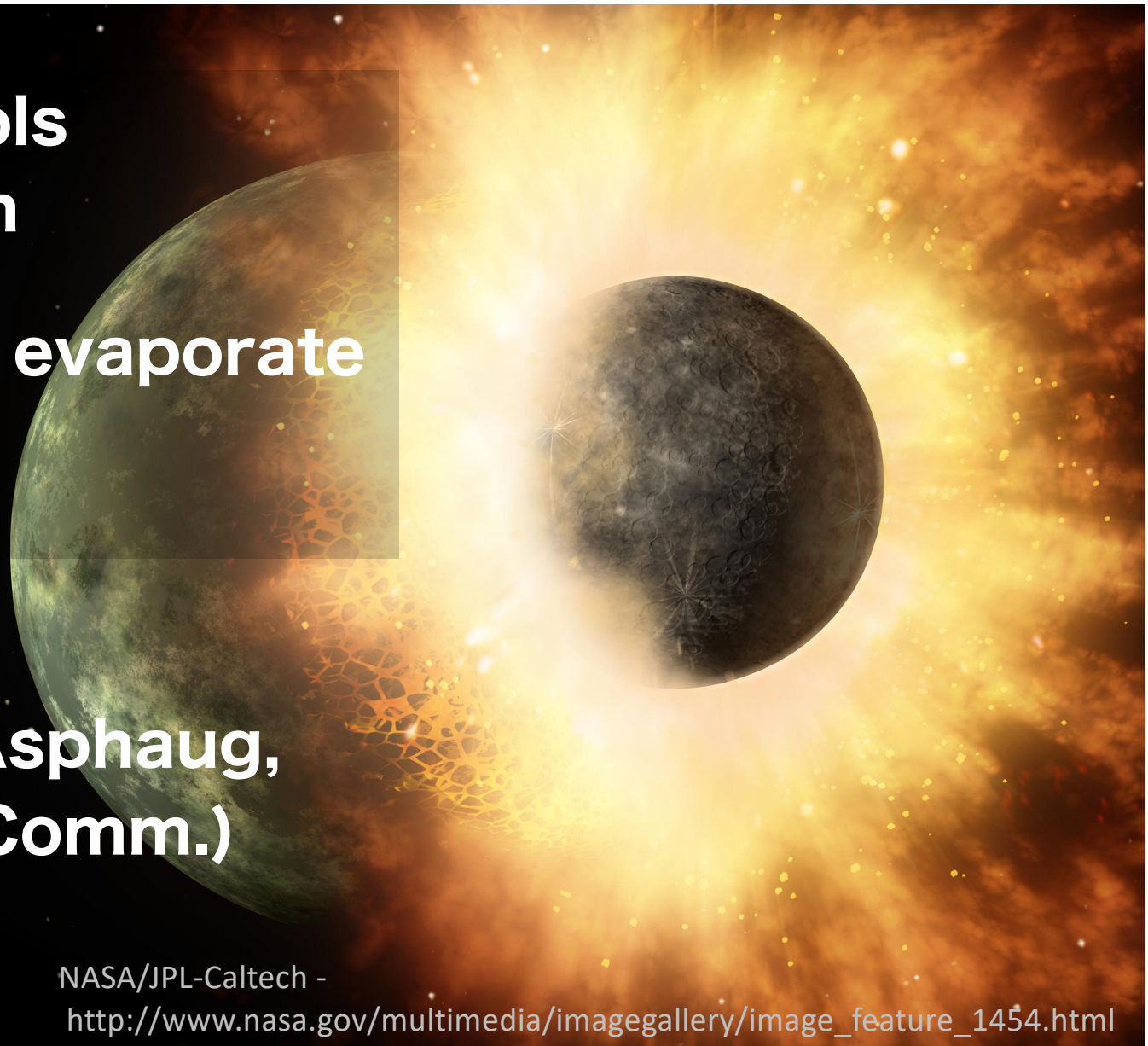
**Evaporation controls  
icy moon formation**

**Rocky planets also evaporate  
for  $M_p > 5-6 M_{\text{earth}}$  !  
--> No large moon**

**Nakajima, Genda, Asphaug,  
Ida (2022, Nature Comm.)**

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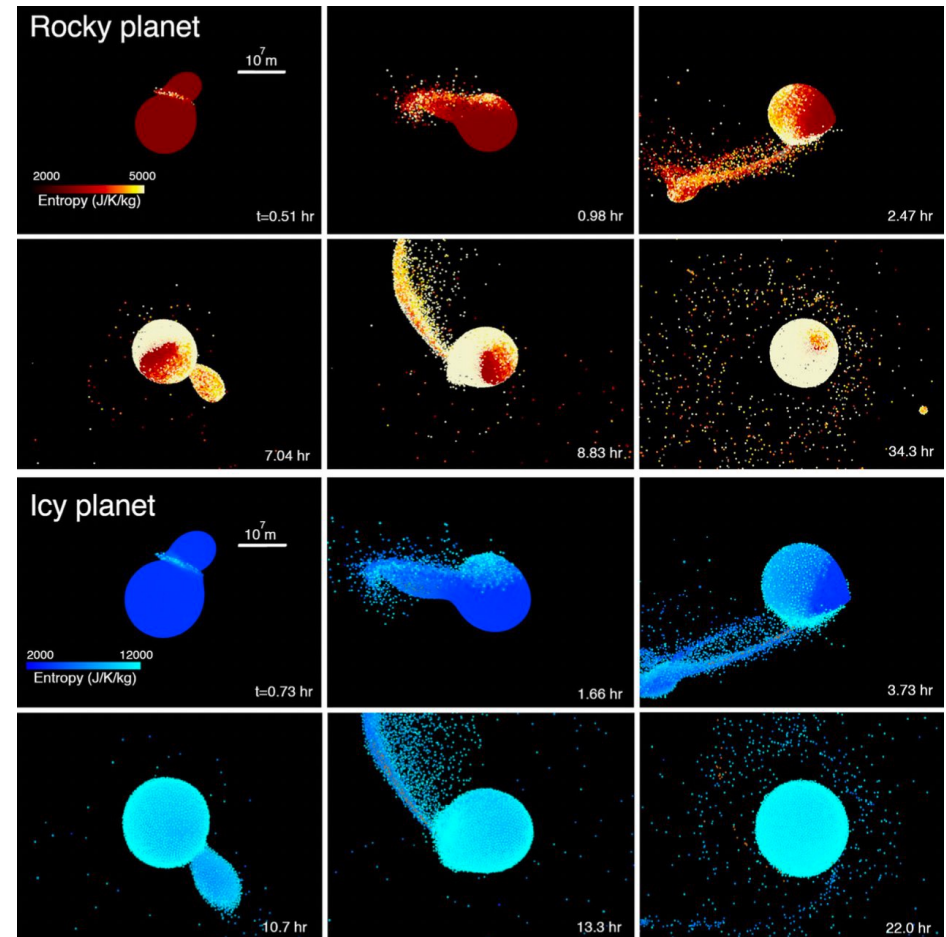
# SPH impact simulation

## ■ latent heat

- rock(silicate) :  $\sim 1 \times 10^7$  J/kg
- water ice:  $\sim 2 \times 10^6$  J/kg

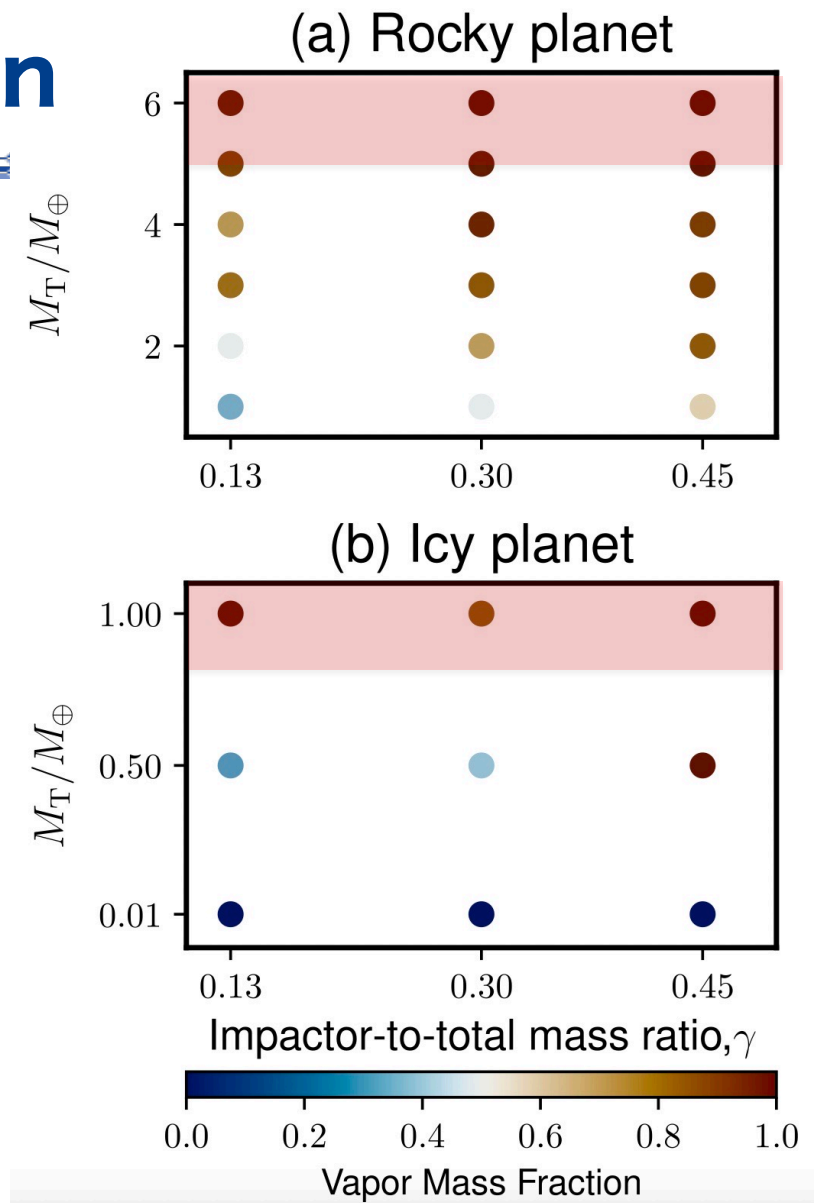
## ■ SPH

- $N = 50K$  or  $100K$
- rocky/icy planets: M-ANEOS + SESAME



# Results: Vapor Mass Fraction

- latent heat
  - rock(silicate) :  $\sim 1 \times 10^7$  J/kg
  - water ice:  $\sim 2 \times 10^6$  J/kg
- VFM  $\sim 1 \rightarrow$  would not have large moons
  - rock :  $> \sim 5-6 M_{\text{earth}}$
  - ice :  $> \sim 1 M_{\text{Earth}}$



# Results: Vapor Mass Fraction

## ■ latent heat

- rock(silicate) :  $\sim 1 \times 10^7$  J/kg
- water ice:  $\sim 2 \times 10^6$  J/kg

## ■ impact energy :

$$\sim 6 \times 10^7 (M/M_{\text{Earth}})^{2/3} (\rho/\rho_{\text{Earth}})^{1/3} \text{ J/kg}$$

## heating energy :

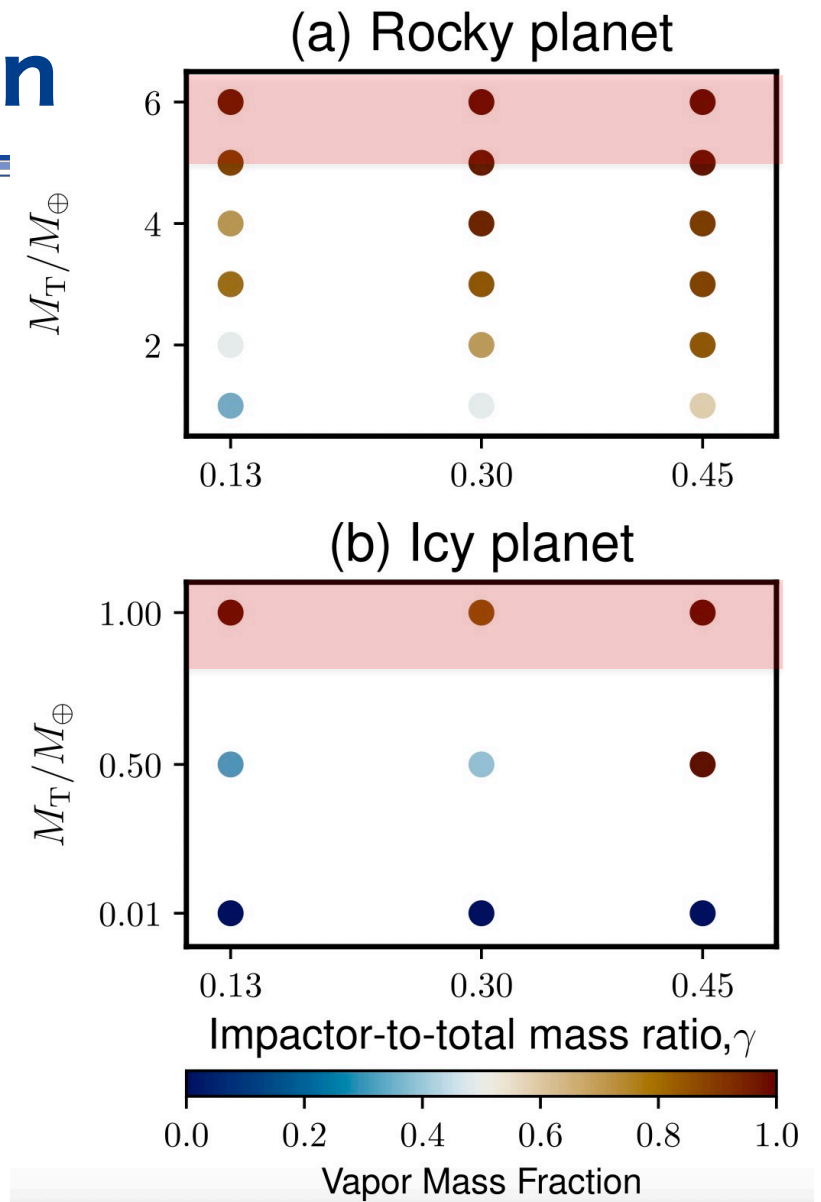
$$\sim 3 \times 10^6 (\varepsilon/0.05) (M/M_{\text{Earth}})^{2/3} (\rho/\rho_{\text{Earth}})^{1/3} \text{ J/kg}$$

efficiency factor

↑ determined by SPH impact simulations

## ■ Exomoons : should be searched around

- rock planets:  $< \sim 5\text{-}6 M_{\text{Earth}}$
- icy planets :  $< \sim 1 M_{\text{Earth}}$





# Summary

- Uranian moons formation by an giant impact
  - disk evolution until ice condensation controls the moon mass & orbit configuration
    - The big difference between Earth's Moon & Uranian moons is explained [fractionally similar impactor mass, but 100 times different moon mass]
- Exomoons formed by giant impacts
  - “totally vaporized or not” is the most important
  - survey should target
    - rock planets:  $< \sim 5-6 M_{\text{Earth}}$
    - icy planets :  $< \sim 1 M_{\text{Earth}}$

